

1

$$\mathcal{L}\{f(t)\} = 1 \quad \mathcal{L}\{1(t)\} = \frac{1}{s} \quad \mathcal{L}\{e^{2t}\} = \frac{1}{s-2}$$

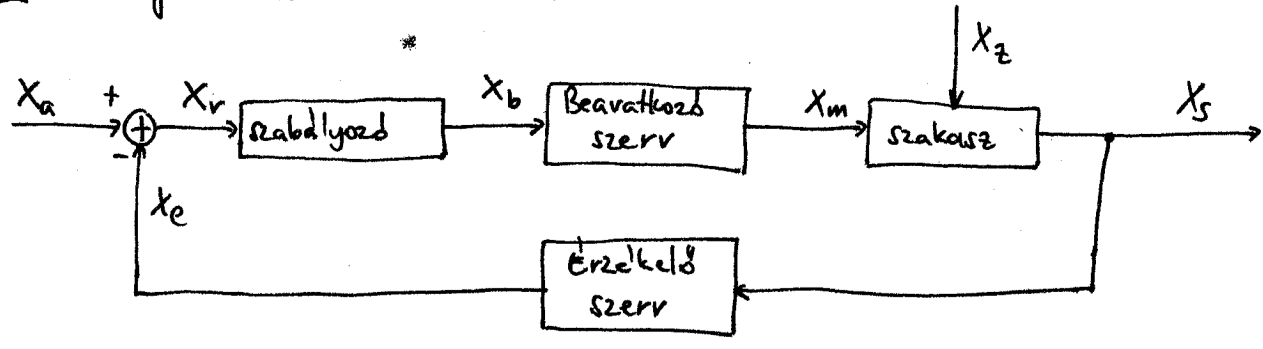
$$\mathcal{L}\{t \cdot e^{3t}\} = \frac{1}{(s-3)^2}$$

2

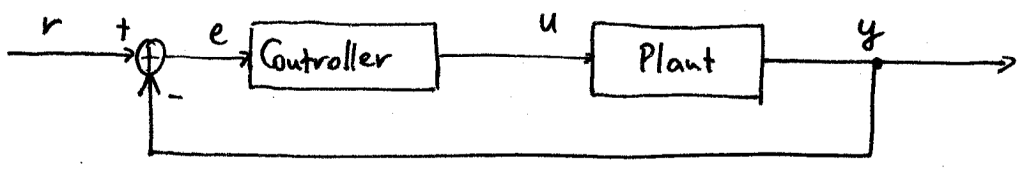
$$\mathcal{L}\{f(t)\} = F(s) \quad \mathcal{L}\{f'(t)\} = s \cdot F(s) - f(0)$$

$$\mathcal{L}\left\{\int_0^{\infty} f(\tau) d\tau\right\} = \frac{F(s)}{s}$$

3 szabványos három blokkvázlata



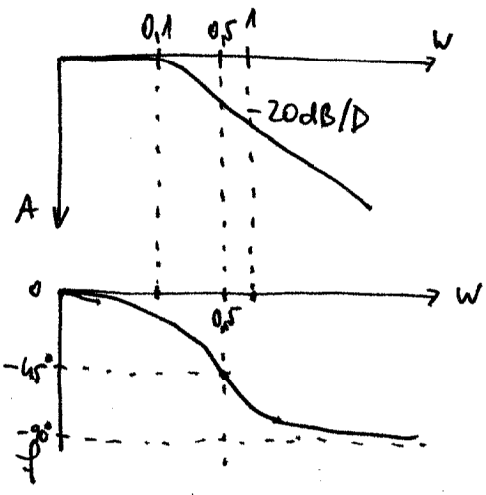
összevonva :



4 egytényelős tag

$$W(s) = \frac{1}{1+T \cdot s}$$

$$p = -\frac{1}{T}$$



$$|A(w)|_{dB} = 20 \lg \frac{1}{\sqrt{1+(wT)^2}}$$

$$\phi(w) = -\arctg(wT)$$

$$w = \frac{1}{T} \rightarrow \phi = -45^\circ$$

$$w = \frac{1}{10T} \rightarrow \phi = -5^\circ$$

$$w = \frac{10}{T} \rightarrow \phi = -85^\circ$$

5) egytanhelyes tag átmeneti fgv

$$W(s) = \frac{1}{1+sT} = \frac{1}{T} \cdot \frac{1}{s + \frac{1}{T}}$$

$$Y(s) = W(s) \cdot U(s) = \frac{1}{s} \cdot \frac{1}{T} \cdot \frac{1}{s + \frac{1}{T}}$$

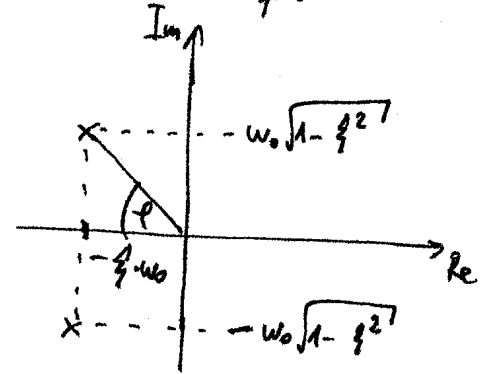
$$u(t) = 1(t) \rightarrow U(s) = \frac{1}{s}$$

$$v(t) = 1(t) - e^{-\frac{t}{T}}$$

$$\mathcal{L}^{-1}\{Y(s)\} = \frac{1}{T} \cdot \mathcal{L}^{-1}\left\{\frac{1}{s} - \frac{1}{s + \frac{1}{T}}\right\}$$

6) kétféle tag átmeneti fgv, rezonancia

$$W(s) = \frac{1}{1 + 2 \cdot \xi \cdot T \cdot s + T^2 s^2} = \frac{\omega_0^2}{\omega_0^2 + 2 \cdot \xi \cdot \omega_0 \cdot s + s^2}$$



$$s_{1,2} = -\xi \omega_0 \pm j \omega_0 \sqrt{1 - \xi^2}$$

rezonancia van, ha $0 \leq \xi < \frac{\sqrt{2}}{2}$

hüllő van, ha $0 \leq \xi < 1$

7) kétféle tag átmeneti fgv

$$v(t) = 1 - \frac{e^{-\xi \omega_0 t}}{\sqrt{1 - \xi^2}} \sin(\omega_0 \sqrt{1 - \xi^2} t + \arccos \xi)$$

$$T_m = \frac{\pi}{\omega_0 \sqrt{1 - \xi^2}}$$

$$\Delta v = v(T_m) - 1 = e^{\frac{-\pi \xi}{\sqrt{1 - \xi^2}}}$$

8) kétféle tag átmeneti fgv

$$T_{\alpha\%} = \frac{\ln \frac{100}{\alpha}}{\sigma_e}$$

9) kétféle tag általános átmeneti fgv

$$s_{1,2} = -\frac{1}{\sqrt{2T}} \pm j \frac{1}{\sqrt{2T}}$$

$$s_{1,2} = -\xi \omega_0 \pm j \omega_0 \sqrt{1 - \xi^2}$$

$$\omega_0 = \frac{1}{T}$$

$$\frac{1}{\sqrt{2T}} = \xi \cdot \frac{1}{T}$$

$$\frac{1}{\sqrt{2}} = \omega_0 \frac{1}{T} \sqrt{1 - \xi^2}$$

$$\xi = \frac{1}{\sqrt{2}} \quad T = 1$$

10) folytonosidejű LTI állapotegyenlete

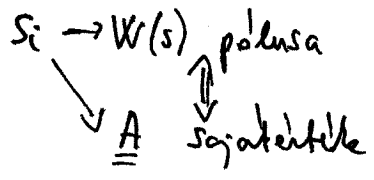
$$\dot{X} = A \cdot X + B \cdot u$$

$$Y = C \cdot X + D \cdot u$$

$$s \cdot X(s) = A \cdot X(s) + B \cdot u(s) \quad W(s) = \frac{Y(s)}{u(s)}$$

$$Y(s) = C \cdot X(s) + D \cdot u(s)$$

$$u(s) = (sI - A) \cdot X(s) \quad W(s) = C \cdot (sI - A)^{-1} \cdot B + D$$



11) $W(s) = \frac{2}{s+10}$

$s_1 = -10$ - pólus

$$V(s) = \frac{2}{s(s+10)} = \frac{0,2}{s} - \frac{0,2}{s+10}$$

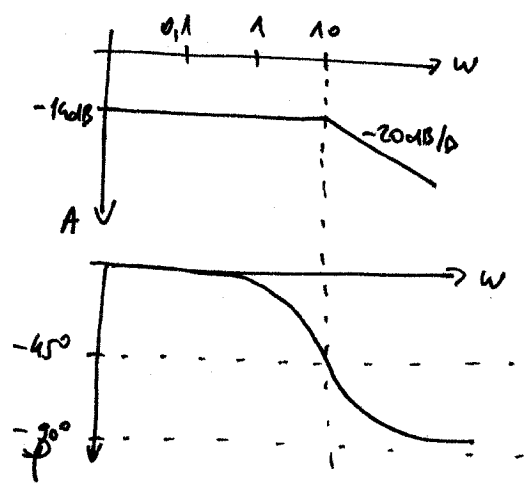
$$v(t) = 0,2 \cdot 1(t) - 0,2 e^{-\frac{t}{10}} \cdot 1(t) - \text{átmeneti fgv}$$

dc = 0,2 - stat. érték

Zpk k-ra az átmeneti (w(t)) fgv konstansát adja, míg a stat. értéket az átmeneti fgv (v(t)) végértékét adja

12) $W(s) = \frac{2}{s+10} \rightarrow \frac{1}{T} = 10 \rightarrow T = 0,1$ $\omega_0 = 10$

$$\varphi(\omega) = -\arctg(\omega T)$$



13) $W(s) = \frac{s+1}{s^2 + \sqrt{2}s + 1}$

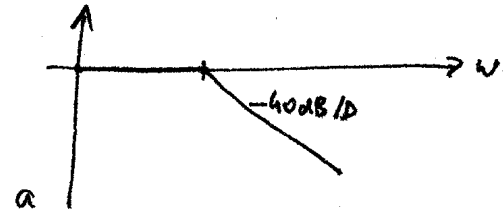
$s_{z_1} = -1$

$$s_{p_{1,2}} = -\frac{1}{\sqrt{2}} \pm j \frac{1}{\sqrt{2}} = -\frac{\varphi}{T} \pm j \frac{\varphi}{T} \sqrt{1 - \varphi^2}$$

$T = 1 \quad \varphi = \frac{1}{\sqrt{2}}$

14 $W(s) = \frac{1}{s^2 + \sqrt{2}s + 1}$

$\varphi(\omega=0) = 0^\circ$
 $\varphi(\omega=\infty) = -k \cdot 90^\circ = -180^\circ$

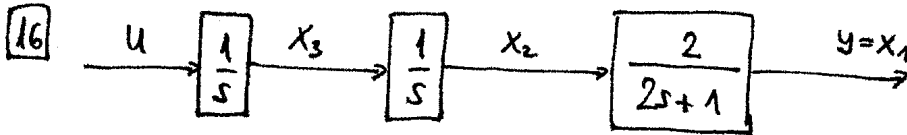


15 $\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix} = \begin{bmatrix} -1 & 2 \\ 1 & 0 \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} 1 \\ 0 \end{pmatrix} \cdot u$

$(-1-\lambda)(-\lambda) - 2 = 0$
 $\lambda^2 + \lambda - 2 = 0$

$\lambda_1 = -2 = s_{p1}$
 $\lambda_2 = 1 = s_{p2}$

$y = x_1$



$W(s) = \frac{2}{s^2(2s+1)}$

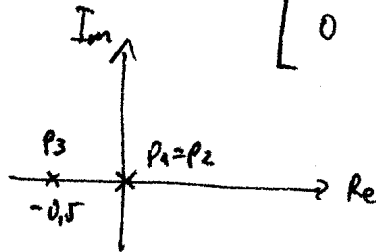
$s_{p1} = s_{p2} = 0$
 $s_{p3} = -\frac{1}{2}$

$\dot{x}_3 = u$
 $\dot{x}_2 = x_3$
 $y = x_1$
 $\dot{x}_1 = -0,5x_1 + x_2$

$(-0,5-\lambda)(-\lambda)(-\lambda) = 0$
 $\lambda^3 + 0,5\lambda^2 = 0$

$\lambda_1 = \lambda_2 = 0$ $\lambda_3 = -0,5$

$A = \begin{bmatrix} -0,5 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$



17 allepolter (s):

$\dot{x} = Ax + Bu$ ss 2 tf
 $y = C \cdot x + D \cdot u$ ss 2 zp

strikeli fgv (tf):
 rationale list
 altham

$\frac{b_0 s^m + b_1 s^{m-1} + \dots + b_m}{s^n + a_1 s^{n-1} + \dots + a_n}$ (m < n) tf 2 ss
 tf 2 zp

strikeli fgv (zpf)
 gjoelldngesie

$k \frac{\prod_{i=1}^m (s - z_i)}{\prod_{j=1}^n (s - p_j)}$ zp 2 tf
 zp 2 ss